4.1 4.2 Congruency

#### Congruency:

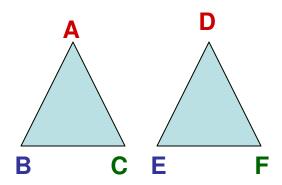
Congruent figures \_\_\_\_\_

•

If  $\triangle ABC \cong \triangle DEF$  then:

<u>Angles</u>

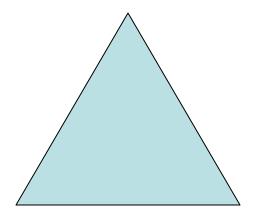
<u>Sides</u>

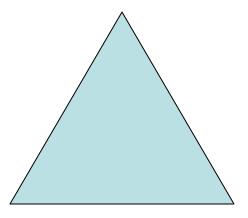


In a proof, if triangles are congruent and you plan to prove that corresponding pieces are congruent use:							

#### Reasons for Proving Triangles Congruent

Postulate 12:





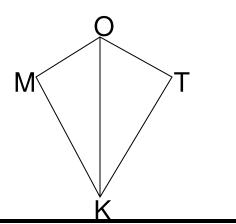
Postulat	e 13:	

Postulate	e 14:	

Given: OK bisects ∠MOT

 $\overline{OM} \cong \overline{OT}$ 

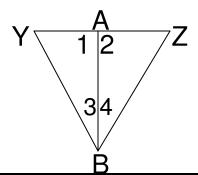
Prove :  $\angle MKO \cong \angle TKO$ 



*Given*:  $\overline{BA} \perp \overline{YZ}$ 

 $\overline{BA}$  bisects  $\angle YBZ$ 

Prove :  $\overline{BY} \cong \overline{BZ}$ 

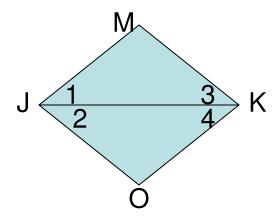


# Proving other Congruencies

Given:  $\overline{MK} \cong \overline{KO}$ 

*KJ* bisects ∠MKO

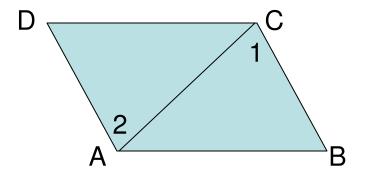
Prove: *KJ* bisects ∠MJO



*Given* :  $\overline{AD} \parallel \overline{BC}$ 

 $\overline{\mathrm{AD}}\cong \overline{BC}$ 

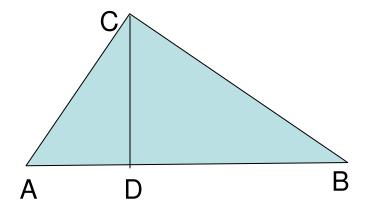
Prove :  $\overline{AB} \cong \overline{CD}$ 



Given:  $\overline{\text{CD}} \perp \overline{AB}$ 

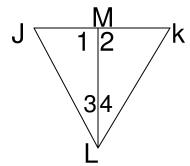
D midpoint AB

Prove :  $\overline{CA} \cong \overline{CB}$ 



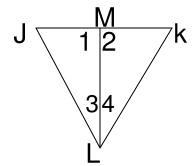
*Given*:  $\angle 1 \cong \angle 2; \angle 3 \cong \angle 4$ 

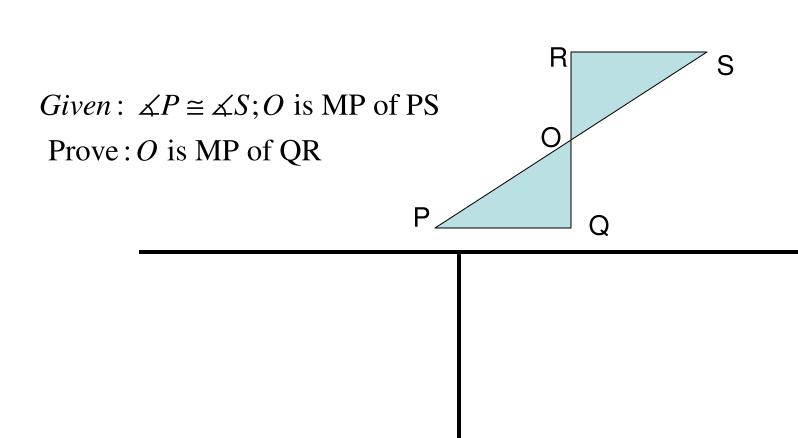
Prove: *M* is midpoint of JK



*Given*:  $\angle 1 \cong \angle 2; \angle 3 \cong \angle 4$ 

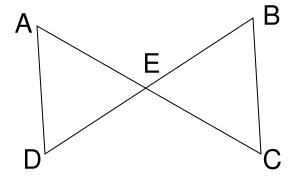
Prove:  $\triangle JKL$  is Isosceles





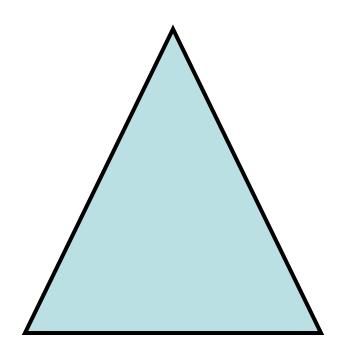
Given:  $\overline{AE} \cong \overline{BE}; \overline{DE} \cong \overline{CE}$ 

Prove :  $\angle D \cong \angle C$ 



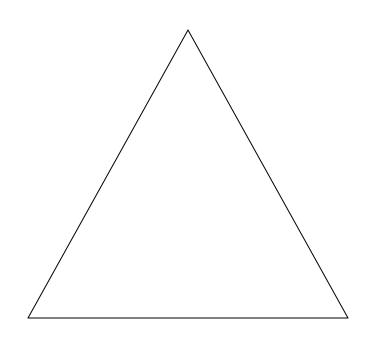
# Isosceles Triangles

### Lets draw an Isosceles Triangle

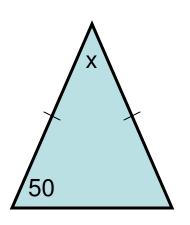


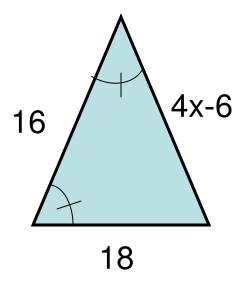
Def of Isosceles Triangle:
•
Theorem 4-1:
Theorem 4-2:

Corollary 2:			



# Examples:



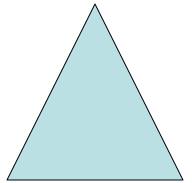


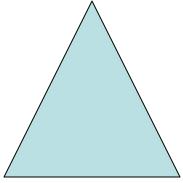
X=\_

# Triangles Congruent

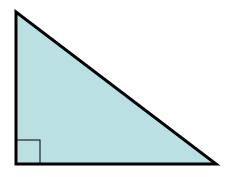
#### More Ways to Prove Triangles Congruent

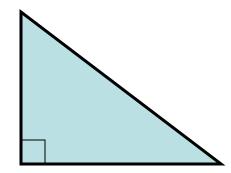
Theorem 4.3:



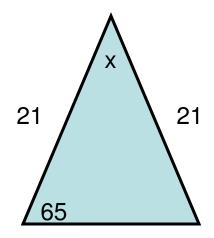


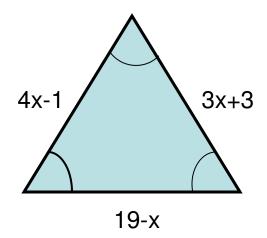
Theorem 4	.4:		

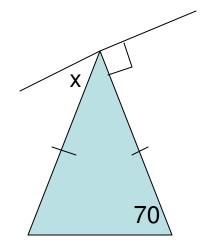


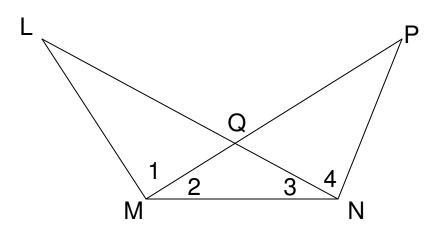


# Examples:





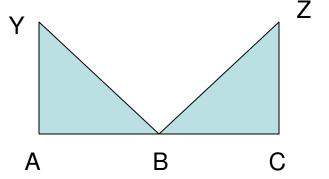




If  $\angle 1 = \angle 2$  and  $\angle 3 = \angle 4$ Name 2 sets of  $\triangle$ 's that are  $\cong$ 

Given:  $\overline{YA} \perp \overline{AC}$ ;  $\overline{ZC} \perp \overline{AC}$ B is Midpoint of  $\overline{AC}$   $\overline{YB} \cong \overline{ZB}$ 

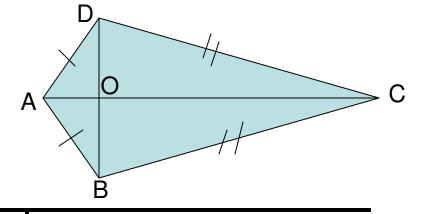
Prove :  $\angle ABY \cong \angle CBZ$ 



# Proving More than one set of Triangles Congruent

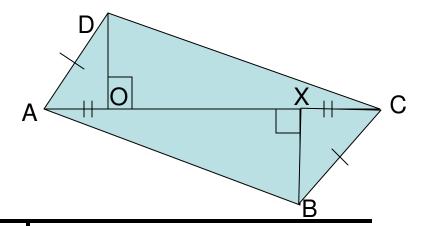
Given: Marked

Prove: O is Midpoint of  $\overline{DB}$ 



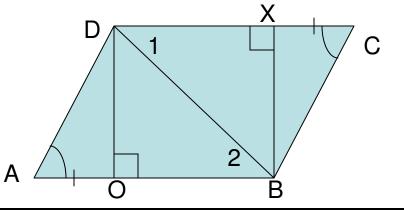
Given: Marked

Prove :  $\overline{DC} \cong \overline{AB}$ 



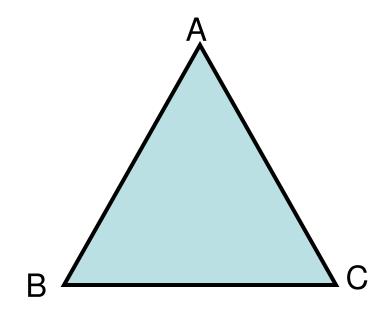
Given: Marked

Prove :  $\overline{DC} \parallel \overline{AB}$ 

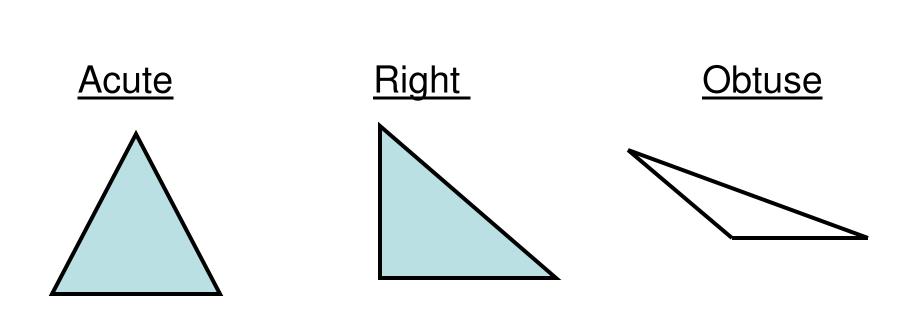


# Altitude, Median and Perpendicular Bisector

Median: _		

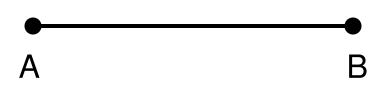


Altitude:		
•		



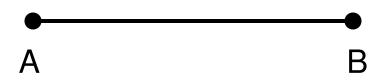
Perpendicular Bisector _	

PBT			
	C		

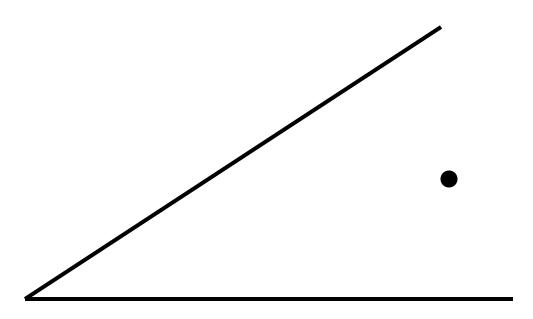


CPBT					





Theorem 4.7:		



Given:  $\angle D \cong \angle B$ ;  $\angle BCO \cong \angle DCO$ 

Prove: OC is the median of  $\triangle DBC$ 

